

## Funcția arccosinus

$$f : [0, \pi] \rightarrow [-1, 1]$$

$$f(x) = \cos x$$

$$g : [-1, 1] \rightarrow [0, \pi]$$

$$g(x) = \arccos x$$

$$f \circ g = 1_{[-1, 1]}$$

$$\cos[\arccos(x)] = x, \forall x \in [-1, 1]$$

$$g \circ f = 1_{[0, \pi]}$$

$$\arccos(\cos(x)) = x, \forall x \in [0, \pi]$$

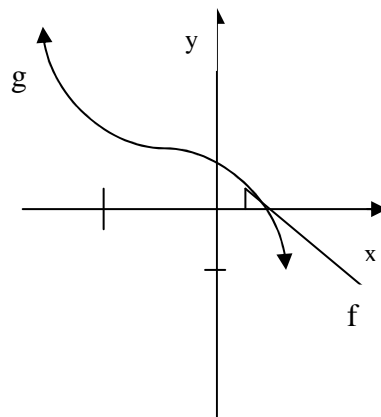
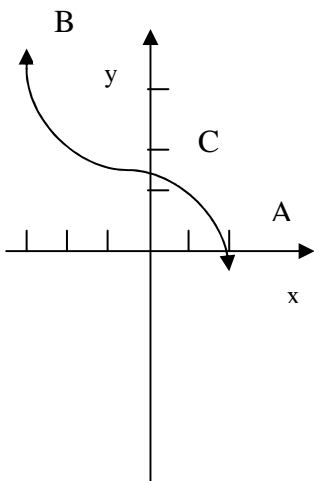
$$\arcsin x + \arccos x = \frac{\pi}{2}, \forall x \in [-1, 1].$$

$$\arcsin(-x) = -\arcsin(x), x \in [-1, 1]$$

$$\arccos(-x) = \pi - \arccos x, \forall x \in [-1, 1]$$

### Graficul funcției arccosinus

x	-1	$-\frac{\sqrt{2}}{2}$	$-\frac{1}{2}$	0	$\frac{1}{2}$	$\frac{\sqrt{2}}{2}$	1
g(x)	$\pi$	$\frac{3\pi}{4}$	$\frac{2\pi}{3}$	$\frac{\pi}{2}$	$\frac{\pi}{3}$	$\frac{\pi}{4}$	0



## Proprietatile functiei arccos:

### 1) Intersectia gf cu axele de coordonate :

$$G_g \cap Ox : y = 0 \rightarrow x = 1, A(1,0)$$

$$G_g \cap Oy : x = 0 \rightarrow y = \frac{\pi}{2}, C(0, \frac{\pi}{2})$$

### 2) Paritatea :

$$\text{- nu, } \arccos(-x) = \pi - \arccos x, \forall x \in [-1,1]$$

### 3) Simetria graficului:

$$\text{- in raport cu punctul } C(0, \frac{\pi}{2})$$

$$\frac{\pi}{2} = \frac{\arccos(-x) + \arccos x}{2}, \forall x \in [-1,1]$$

### 4) Monotonia functiei:

$$\text{- strict crescatoare pe } [-1,1]$$

### 5) Marginire. Valori extreme:

$$\text{- functie marginita, } 0 \leq g(x) \leq \pi$$

$$\text{- min } g(x) = 0 = g(1), A(1,0);$$

$$\text{- max } g(x) = \pi = g(-1), B(-1, \pi)$$

### 6) Convezitate si concavitate:

$$\text{- convexa pe } [-1,0]$$

$$\text{- concave pe } [0,1]$$

$$\text{- } x=0, \text{ punct de inflexiune pentru functie}$$

### 7) Continuitate:

$$\text{- curba continua}$$

### 8) Rezolvarea ecuatiei g(x)=0:

$$\text{- } \arccos x = 0 \Leftrightarrow x = 1$$

### 9) Semnul functiei:

$$\text{- } \arccos x > 0, \forall x \in [-1,1]$$

### 10) Bijectivitatea

$$\text{- da}$$

### 11) Functia inversa

$$f : [0, \pi], f(x) = \cos x,$$

$$\text{- } \cos(\arccos x) = x, \forall x \in [-1,1]$$

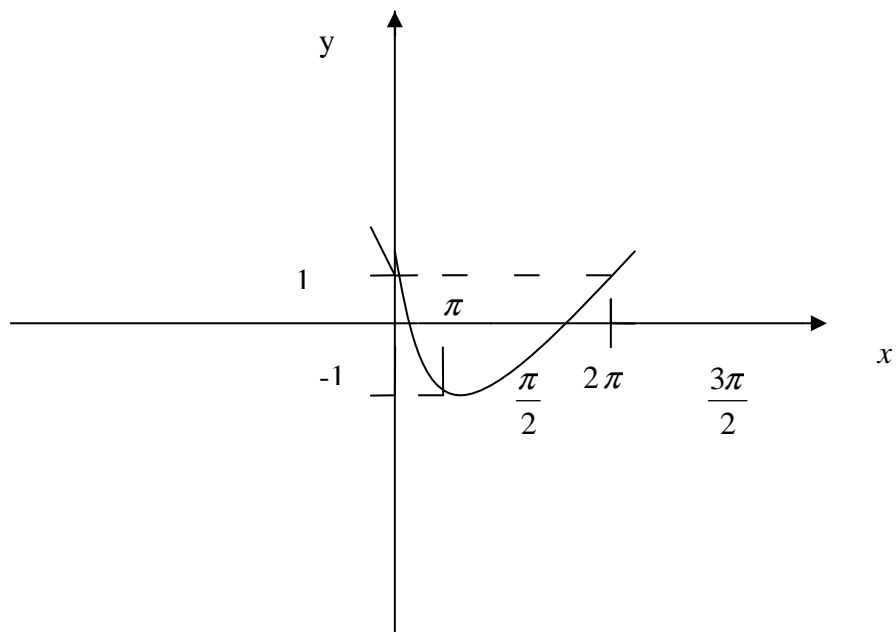
$$\text{- } \arccos(\cos x) = x, \forall x \in [0, \pi]$$

## Funcția cosinus

$$f : \mathbb{R} \rightarrow [-1,1], f(x) = \cos x$$

Graficul funcției cosinus.

x	0	$\frac{\pi}{2}$	$\pi$	$\frac{3\pi}{2}$	$2\pi$
f(x)=cos x	1	0	-1	0	1



Proprietati:	pe $[0, 2\pi]$	pe $\mathbb{R}$												
1) Intersectia graficului cu axele de coordonate:	$x=0 \rightarrow f(0)=1, A(0,1)$	$A(0,1)$												
$G_f \cap Oy :$	$y=0 \rightarrow x_1 = \frac{\pi}{2}, x_2 = \frac{3\pi}{2}$	$(\frac{\pi}{3} + 2k\pi, 0)$ $(\frac{3\pi}{2} + 2k\pi, 0)$												
$G_f \cap Ox :$	$B(\frac{\pi}{2}, 0), D(\frac{3\pi}{2}, 0)$													
2) Paritate	_____	para $f(x)=f(x), x \in \mathbb{R}$												
3) Simetria Graficului	_____	in raport cu axa Oy												
4) Monotonie:	<table style="display: inline-table; border-collapse: collapse;"> <tr> <td style="border-right: 1px solid black; padding: 5px;"><math>x</math></td> <td style="padding: 5px;"><math>0</math></td> <td style="padding: 5px;"><math>\frac{\pi}{2}</math></td> <td style="padding: 5px;"><math>\pi</math></td> <td style="padding: 5px;"><math>\frac{3\pi}{2}</math></td> <td style="padding: 5px;"><math>2\pi</math></td> </tr> <tr> <td style="border-right: 1px solid black; padding: 5px;"><math>f(x)</math></td> <td style="padding: 5px;"><math>1</math></td> <td style="padding: 5px;"><math>0</math></td> <td style="padding: 5px;"><math>-1</math></td> <td style="padding: 5px;"><math>0</math></td> <td style="padding: 5px;"><math>1</math></td> </tr> </table>	$x$	$0$	$\frac{\pi}{2}$	$\pi$	$\frac{3\pi}{2}$	$2\pi$	$f(x)$	$1$	$0$	$-1$	$0$	$1$	pe $[2k\pi, \pi + 2k\pi]$ , pe $[\pi + 2k\pi, 2\pi + 2k\pi]$
$x$	$0$	$\frac{\pi}{2}$	$\pi$	$\frac{3\pi}{2}$	$2\pi$									
$f(x)$	$1$	$0$	$-1$	$0$	$1$									
Strict crescatoare <span style="font-size: 2em; vertical-align: middle;">↗</span>	pe $[0, \pi], f, \text{este.s.d}$													
Strict descrescatoare <span style="font-size: 2em; vertical-align: middle;">↘</span>	pe $[\pi, 2\pi], f, \text{este.s.c}$													
5) Marginire valori extreme	$-1 \leq f(x) \leq 1$ $\max, f(x) = 1 = f(0), A(0,1)$ $\min, f(x) = -1 = f(x), C(\pi, -1)$	$-1 \leq f(x) \leq 1$ $\max, f(x) = -1$ $= f(\pi + 2k\pi)$												
6) Convexitate si concavitate	concave pe $[0, \frac{\pi}{2}], [\frac{3\pi}{2}, 2\pi]$ convexa pe $[\frac{\pi}{2}, \frac{3\pi}{2}]$	$[-\frac{\pi}{2} + 2k\pi, k \in \mathbb{Z}]$ $[\frac{\pi}{2} + 2k\pi, \frac{3\pi}{2} + 2k\pi]$												
7) Continuitate	Curba continua	Curba continua												
8) Rezolvarea ecuatiei $f(x)=0$	$x_1 = \frac{\pi}{2}, x_2 = \frac{3\pi}{2}$	$x_{1,k} = \frac{\pi}{2} + 2k\pi,$ $x_{2,k} = \frac{3\pi}{2} + 2k\pi,$												

9) Semnul functiei	$\cos x > 0 \quad x \in [0, \frac{\pi}{2}) \cup (\frac{3\pi}{2}, 2\pi)$ $\cos < 0 \quad x \in (\frac{\pi}{2}, \frac{3\pi}{2})$	$x \in (\frac{\pi}{2} + 2k\pi, \frac{3\pi}{2} + 2k\pi)$ $x \in (-\frac{\pi}{2} + 2k\pi, \frac{\pi}{2} + 2k\pi)$
10) Bijectivitatea	nu	nu
11) Restrictie bijectiva	$[0, \pi]$	$[2k\pi, \pi + 2k\pi], k \in \mathbb{Z}$